

Accuracy Load Flow Of Iraqi 400 Kv supper Grid

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Abstract ---The aim of this paper is to develop a mathematical model and a computer program to determine the limits of load flow result deviation for electrical power network. This work basically a comparison consists of load flow method Newton Raphson and fast decoupled .The comparison concerns the voltage magnitude, voltage angle, the generated reactive power of PV -buses and the active and reactive power losses. The accuracy of the fast decoupled method tested compared to the classical N-R considering the operative Iraqi national network (400 KV) power grid as a test case. The programs used in this work are implemented using (MATLAB).

1 INTRODUCTION

The great importance of load-flow studies is in planning the future expansion of power system as well as in determining the best operation of existing systems. The principal information obtained from a load-flow study is the magnitude and phase angle of the voltage of each bus and the real and reactive power flowing in each line .However much additional information or volume is provided by the printout of the solution from computer programs use by the power companies [1].

Either the bus self-and mutual admittance's which compose the bus admittance matrix Y_{bus} or the driving-point and transfer impedance which compose Z_{bus} may be used in solving the load-flow problem [2]. We shall confine our study to methods using admittance's.

The starting point in obtaining the data, which must be furnished to the computer, is the one-line diagram of the system. Values of series impedance's and shunt admittance's of transmission lines are necessary so that the computer can determine all the Y_{bus} or Z_{bus} elements. Other essential information includes transformer ratings and impedances , shunt capacitor ratings, and transformer tap settings.

Operating loading condition must always be selected for the study. At each bus except one the net real power into the network must be specified .

The power drawn by a load is negative power input to the system. The other power input are from generators and positive or negative power entering over interconnections. In addition at these buses either the net flow of reactive power into the network or the magnitude of the voltage must be specified; that is at each bus a decision is required whether the voltage magnitude or the reactive-

Depending upon which two variables are specified a priori, the buses are classified into three categories:-

(i)PQ bus: At this type of bus, the net powers P_i and Q_i are known (P_{Di} and Q_{Di} are known from load forecasting and P_{Gi} and Q_{Gi} are specified) . The unknowns are V_i and [5] .

(ii)PV bus: At this type of bus P_{Di} and Q_{Di} are known a priori and V_i and P_i (hence P_{Gi}) are specified .The unknowns are Q_i (hence Q_{Gi}) and.

(iii)slack bus: This bus is distinguished from the other two types of buses by the fact that real and reactive power at this bus is not specified. Instead voltage magnitude and phase angle are specified [3].

The main goal in this work is to devise and quantify the accuracy of a certain approximated load flow method compared to a standard classical one. The classical method consideration here is the standard Newton-Raphson in polar form. The approximate method studied here is the fast - decoupled load flow.

The most important mathematical operation in power system analysis is the investigation of load-flows. A load-flow study is concerned with the determination of the state variables (voltage, current, power, and power factor) at the various points of the power network. Load-flow studies are essential for all power system problems, and it is not a simple task. No direct solution can be found, to a load-flow problem because of the nature of the equations and the ever increasing complexity of power systems. Therefore, iterative techniques of solution are conventionally used in this respect [4].

Performance equations for a load-flow study (load-

flow methods) are usually derived on the basis of nodal or bus frame of reference. The use of the nodal or bus frame of reference greatly simplifies the preparation of data; and the effects of shunt elements to ground may be easily included.

At each node of the power network, there are four variables; the real power, the reactive power, the voltage magnitude, and the phase shift. The four variables can be combined in a mathematical complex equation which can be resolved into two real equations. It is thus necessary to specify two variables per node to completely solve for the network state.

An early approach to load-flow problem solution was the Gauss-Seidel iterative method using the nodal admittance matrix and this was further improved by using the nodal impedance matrix. The Gauss-Seidel method is basically a straight substitution and correction process. It is used for small systems due to its slow convergence and low computer storage requirements [4].

Newton Raphson's method using the nodal admittance matrix has gained widespread popularity because of its quadratic convergence characteristics in load flow analysis. Its iterative process is summarized as follows: At each stage of the process, a set of nonlinear algebraic equations are linearized about the point representing current values of bus voltages, and a set of linear equations is solved to obtain a better solution of bus voltages. It is basically used for large well-conditioned power systems due to its fast convergence and accurate solution.

Numerical methods are generally at their most efficient use when they take advantage of the physical properties of the system being solved. Hence, for example, the exploitation of network sparsely by ordered elimination and skilful programming has been used in the Newton's method to improve the speed and storage capacity. Recently, attention has been given to the exploitation of the loose physical interaction between MW and Mvar flows in a power system, by mathematically decoupling the MW-θ and Mvar-V calculations [3].

In a decoupled Newton-method, (a) the convergence of this method is faster than that of the Newton method in the early stages of the solution, (b) the method does not lead to high accurate solution, and (c) It has a high degree of reliability and needs low storage.

There are many powerful methods For load-Flow study, but the fast decoupled load flow method (FDLF) has been accepted in recent

years by the utility industry as the best approach to obtain the power flow solutions. The FDLF method is used in system planning, operational planning and operational control this is due to its low memory requirements speed and very good convergence characteristics for practical problems [5].

2 DERIVATION OF ALGORITHMS :

The complex power injected by the source into the ith bus of a power system is :

$$S_i = P_i + jQ_i = V_i I_i^* \quad , \quad i = 1, 2, \dots, n \quad \dots (1)$$

Where V_i is the voltage at the ith bus with respect to ground and I_i is the source current injected into the bus.

The load flow problem is handled more conveniently by use of I_i rather than I_i^* .

Therefore, taking the complex conjugate of eq : (2), we have :

$$P_i - jQ_i = V_i^* I_i \quad , \quad i = 1, 2, \dots, n \quad \dots (2)$$

Real and reactive power can now be expressed as :

$$P_i(\text{real power}) = |V_i| \sum_{k=1}^n |V_k| |Y_{ik}| \cos(\theta_{ik} + \delta_k - \delta_i) ; i = 1, 2, \dots, n \quad \dots (5)$$

$$Q_i(\text{reactive power}) = -|V_i| \sum_{k=1}^n |V_k| |Y_{ik}| \sin(\theta_{ik} + \delta_k - \delta_i) ;$$

Equations (5) and (6) represent 2n power flow equations at n buses of a power system. For the derivation of algorithms, the power system admittance matrix is taken as a convenient starting point. The bus admittance matrix which describes the net injected currents as a function of bus voltages can be written as:

$$[I_{bus}] = [Y_{bus}][V_{bus}] \dots \dots \dots (7)$$

Injected power at each bus k can be written as:

$$P_k^{cal} = \text{Re} \left(V_k \sum_{i=1}^n Y_{ki}^* V_i \right) \\ = V_k \sum_{i=1}^n V_i (G_{ki} \cos \theta_{ki} + B_{ki} \sin \theta_{ki}) \dots \dots \dots (8)$$

We now applying to power-flow problem the four Newton-Raphson steps, starting with [7].

$$x^r = \begin{bmatrix} \delta^r \\ V^r \end{bmatrix} \text{ at the } r\text{th iteration.}$$

Step 1:

Using Eq. (2.19) and Eq. (2.20) to compute

$$\Delta y^r = \begin{bmatrix} \Delta p^r \\ \Delta Q^r \end{bmatrix} = \begin{bmatrix} P - P(x^r) \\ Q - Q(x^r) \end{bmatrix} \quad (15)$$

Step 2:

Using the equation in table 1 to calculate the Jacobian matrix.

Step 3:

Using Gauss elimination and back substitution to solve

$$\begin{bmatrix} j_1^r & j_2^r \\ j_3^r & j_4^r \end{bmatrix} \begin{bmatrix} \Delta \delta^r \\ \Delta V^r \end{bmatrix} = \begin{bmatrix} \Delta P^r \\ \Delta Q^r \end{bmatrix} \quad \dots\dots\dots (16)$$

Step 4:

Computing

$$x^{r+1} = \begin{bmatrix} \delta^{r+1} \\ V^{r+1} \end{bmatrix} = \begin{bmatrix} \delta^r \\ V^r \end{bmatrix} + \begin{bmatrix} \Delta \delta^r \\ \Delta V^r \end{bmatrix} \quad \dots\dots\dots (17)$$

Starting with initial value V0, the procedure continues until convergence is obtained or until the number of iterations exceeds a specified maximum. Convergence criteria are often based on (Δy^r) called power mismatches.

4 FAST DECOUPLED POWER FLOW METHOD

The fast decoupled power flow method is a very fast and efficient method of obtaining power flow problem solution. In this method, both, the speeds as well as the sparsity are exploited. This is

actually an extension of Newton-Raphson method formulated in polar coordinates with certain approximations which result into a fast algorithm for power flow solution. This method exploits the property of the power system where in MW flow-voltage angle and Mvar flow-voltage magnitude are loosely coupled. In other words a small change in the magnitude of the bus voltage does not affect the real power flow at the bus and similarly a small change in phase angle of the bus voltage has hardly any effect on reactive power flow. Because of this loose physical interaction between MW and Mvar flows in a power system, the MW- δ and Mvar-V calculations can be decoupled .

This decoupling results in a very simple, fast and reliable algorithm. As already said in the preceding article. The sparsity feature of admittance matrix minimizes the computer memory requirements and results in faster computations. The accuracy is comparable to that of the N-R method .

The earlier equation of power flow studies and according to Newton-Raphson method that represented by:

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} J_1 & J_2 \\ J_3 & J_4 \end{bmatrix} \begin{bmatrix} \Delta \delta \\ \Delta V \end{bmatrix}$$

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} H & N \\ M & L \end{bmatrix} \begin{bmatrix} \Delta \delta \\ \Delta V \end{bmatrix} \quad \dots\dots\dots (18)$$

where H, N, M and L are the elements (J1 J2, J3 and J4) of the Jacobian matrix. Since changes in real power (i.e., ΔP) is less sensitive to the changes in voltage magnitude (i.e., ΔV) and changes in reactive power (i.e., ΔQ) is less sensitive to the changes in phase angle of voltage (i.e. $\Delta \delta$) equation (18) can be reduced to:

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} H & 0 \\ 0 & L \end{bmatrix} \begin{bmatrix} \Delta \delta \\ \Delta V \end{bmatrix} \quad \dots\dots\dots (19)$$

The equations (19) are decoupled equations and can be expanded as:

$$\Delta P = H * \Delta \delta \quad \dots\dots\dots (20)$$

$$\Delta Q = L * \Delta V \quad \dots\dots\dots (21)$$

The next step in deriving the algorithm is to make suitable assumptions in deriving the expressions for H and L.

Off-diagonal element of H is:

$$\begin{aligned}
 H_{ik} &= \frac{\partial P_i}{\partial \delta_k} = V_i V_k Y_{ik} \sin(\theta_{ik} + \delta_i - \delta_k) \\
 &= V_i V_k Y_{ik} \left[\sin \theta_{ik} \cos(\delta_i - \delta_k) + \cos \theta_{ik} \sin(\delta_i - \delta_k) \right] \\
 &= V_i V_k \left[Y_{ik} \sin \theta_{ik} \cos(\delta_i - \delta_k) + Y_{ik} \cos \theta_{ik} \sin(\delta_i - \delta_k) \right] \\
 &= V_i V_k \left[-B_{ik} \cos(\delta_i - \delta_k) + G_{ik} \sin(\delta_i - \delta_k) \right] \dots\dots\dots(22)
 \end{aligned}$$

Similarly off-diagonal element of L is:

$$\begin{aligned}
 L_{ik} &= \frac{\partial Q_i}{\partial V_k} = V_i V_k Y_{ik} \sin(\theta_{ik} + \delta_i - \delta_k) \\
 &= V_i V_k \left[G_{ik} \sin(\delta_i - \delta_k) - B_{ik} \cos(\delta_i - \delta_k) \right] \dots\dots\dots(27)
 \end{aligned}$$

From equations (22) and (23), we have

$$H_{ik} = L_{ik} = V_i V_k \left[G_{ik} \sin(\delta_i - \delta_k) - B_{ik} \cos(\delta_i - \delta_k) \right] \dots\dots\dots(24)$$

The diagonal elements of H are given as:

$$\begin{aligned}
 H_{ii} &= \frac{\partial P_i}{\partial \delta_i} = - \sum_{k=1}^n V_i V_k Y_{ik} \left[\sin(\theta_{ik} + \delta_i - \delta_k) \right] \\
 &\quad k \neq i \\
 &= -Q_i + V_i V_k Y_{ii} \sin \theta_{ii} = -Q_i - V_i^2 B_{ii} \dots\dots\dots(24)
 \end{aligned}$$

Similarly diagonal elements for the matrix are given as

$$\begin{aligned}
 L_{ii} &= \frac{\partial Q_i}{\partial V_i} = 2V_i^2 Y_{ii} \sin \theta_{ii} + \sum_{k=1}^n V_i V_k Y_{ik} \sin(\theta_{ik} + \delta_i - \delta_k) \\
 &\quad k \neq i \\
 &= 2V_i^2 Y_{ii} \sin \theta_{ii} + Q_i - V_i^2 Y_{ii} \sin \theta_{ii} \\
 &= Q_i + V_i^2 Y_{ii} \sin \theta_{ii} = Q_i - V_i^2 B_{ii} \dots\dots\dots(25)
 \end{aligned}$$

In the case of fast decoupled power flow method of power flow studies the following approximations are made for evaluating Jacobian elements.

$$\left. \begin{aligned}
 \cos(\delta_i - \delta_k) &\approx 1 \\
 G_{ik} \sin(\delta_i - \delta_k) &\approx B_{ik}
 \end{aligned} \right\}$$

$$\dots\dots\dots(26)$$

$$Q_i \ll B_{ii} V_i^2$$

With the above assumptions the Jacobian elements become

$$\left. \begin{aligned}
 H_{ik} &= L_{ik} = -V_i V_k B_{ik} \text{ for } k \neq i \\
 \text{And } H_{ii} &= L_{ii} = -V_i^2 B_{ii}
 \end{aligned} \right\} \dots\dots\dots(27)$$

With these Jacobian elements equations become

$$\Delta P_i = H \Delta \delta = V_i V_k B_{ik}' \Delta \delta_k \dots\dots\dots(28)$$

$$\text{And } \Delta Q_i = L \Delta V = V_i V_k B_{ik}'' \Delta V_k \dots\dots\dots(29)$$

Where B_{ik}' and B_{ik}'' are elements of $-B_{ik}$ matrix. Further decoupling and final algorithm for the fast-decoupled power-flow studies are obtained by.

- (i) Omitting from B' , the representation of those network elements that affect Mvar flows, i.e., shunt reactances and off-nominal in phase transformer taps.
- (ii) Omitting from B'' , the angle shifting affects of phase shifters.
- (iii) Dividing equations (28) and (29) by V_i and assuming $V_k = 1.0$ p.u and also neglecting series resistance in calculating the elements of B' .

With the above assumptions, equations (30) and (31) for the power flow studies become:

$$\Delta P_i / V_i = B' \Delta \delta \dots\dots\dots(30)$$

And

$$\Delta Q_i / V_i = B'' \Delta V \dots\dots\dots(31)$$

In the above equations B' and B'' are real and sparse and have similar structures as those of H and L respectively. Since, they contain only network admittances, they are constant and do not change during successive iterations for solution of power flow problem, they need to be evaluated only once and inverted once during the first iteration and then used in all successive iterations. It is due to the nature of Jacobian matrices B' and B'' and the sparsity of these matrices that the method is Fast. In this method of power flow studies, each cycle of iteration consists of one solution for $\Delta \delta$ to update δ and one solution for ΔV to update V . The iterations are continued till ΔP and ΔQ at all load buses and ΔP at all generation buses are within prescribed (or assumed)

5 GENERAL

The software package used in this work includes the program (load flow project) which computes voltage magnitude and angle at each bus in a power system balanced three-phase steady-state operation.

To give an indication that the main program used in this study is proper, the computed bus voltages are then used by another program to compute generator, line, and transformer loading.

The bus admittance matrix is calculated from the input data using the following equalities.

For the first iteration, starting values of bus voltage magnitudes and angles are set equal to those of slack bus, except for voltage-controlled busses, whose voltage magnitudes are known. For subsequent iteration with input data changes, the final values of run are used as starting values for the next run.

The Newton-Raphson procedure is terminated when the magnitudes of all power mismatches $\Delta P(r)$ and $\Delta Q(r)$ are less than a tolerance level (typically 0.0001 per unit) or when the number of iterations exceeds a maximum (typically 10). Both the tolerance level and maximum number of iterations are selected by the user.

In the fast Decoupled, the selection of maximum iteration depends on the size of the system.

Bus out data include voltage, real and reactive power of each generator and load, and identification of buses with voltage magnitude more than 5% above or below that of slack bus. Line out data include real and reactive power flows entering the terminals and identification of lines with MVA flows above their maximum ratings. Other useful output include generation, load, and line loss totals, number of iterations to converge, and total mismatches ΔP and ΔQ after convergence. If desired, reactive power delivered by line capacitances or other shunt reactive elements can also be obtained.

The main calculation procedure followed through that this work using the ready provided Matlab subprograms is generally shown in fig. 1

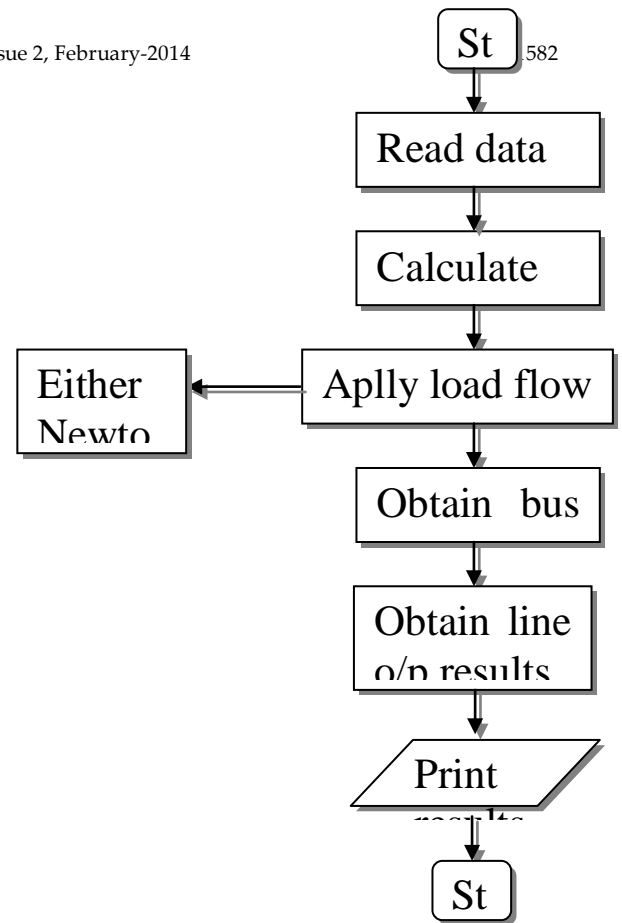


Fig. (1) General procedure Flow chart

6 RESULT AND DISCUSSION

The transmission level in the Iraqi electrical network consists of the 400kV network, (the super grid network) and 132 kV network connected to it. The aim of this work is limited to the 400kV network with all its bus-bars and transmission lines.

The network under consideration consists of 24 bus-bars and 37 transmission lines; with total length at 3711 km. Figure (2) shows a configuration of this network [16].

The model and program which are developed in the previous chapters are applied on the Iraqi super grid network (400kV).

The loads are represented by a static admittance and the lines by the nominal π sections. All network data expressed in per-unit referred to a common base power of 100MVA and common base voltage of 400kV. The results of the network load flow calculations are given in table (1). In the load flow solution, the Baijip.s. station is selected as reference.

Q_{gi} :The generated reactive power in all PV buses

Ploses: The system power active loses. And
 Qloses : The system power reactive loses.

6.3 ACCURACY RESULTS

Table(2)show the deviation (accuracy)of the system bus voltage magnitude for the difference system operating condition .if is interesting to net that the $|V_i|$ is the same under the base condition for both the N-R, and fast decupled load flow. Also it is noted that the two methods almost meet in $|V_i|$ the values the closer the operating condition to the base case and depart as the loading increase.The same observation is noted loading decrease. Figure (3) shows the deviation in plotted form for the result) Accuracy of $|V|$ for Iraqi power grid. Fig (4) shows variation in the voltage angular displacement for the twenty four Iraqi system buses. The method accuracy is sum what differs from that of $|V_i|$ as there are deviations in the base case result too.

Fig.(5) gives the accuracy of the fast decupled method compared to the newton Raphson output the PV buses Q generated the results shows a wide range of variation fig.(5) present the Q generated results.

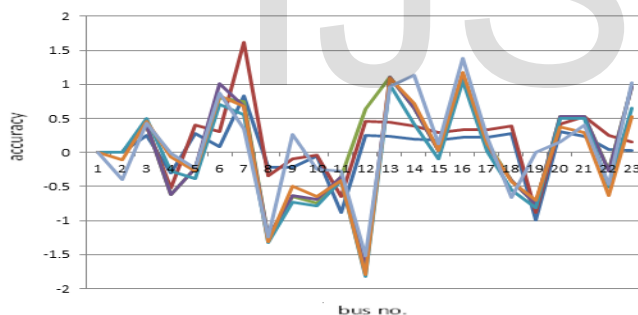


Fig.(3) Accuracy of $|V|$ for Iraqi power grid

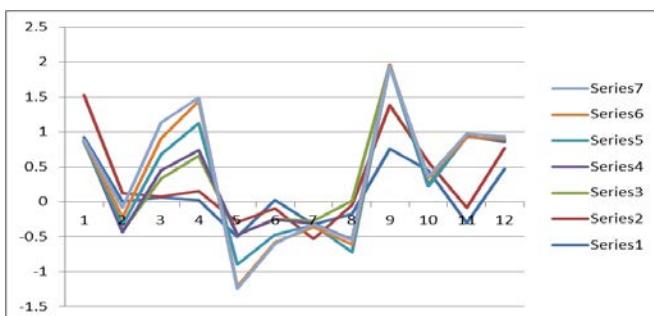


Fig.(4) Accuracy of δ for Iraqi power grid



Fig. (5) Accuracy of Q for Iraqi power grid

7 CONCLUSIONS

a.The fast decupled power flow solution required more iterations than the Newton-Raphson method, but required less time per iteration, and a power flow solution is obtained very rapidly. This technique is very useful in contingency analysis where numerous outages are to be simulated or a power flow solution is required for on-line control.

b.For fixed number of iterations the fast decupled algorithm is not as accurate as the exact Newton-Raphson algorithm. But the saving in computer time is considered more important.

c.A very important limitation for Newton's method is that it dose not generally converge to solution from arbitrary starting point.

d.For large power systems the Newton-Raphson method is found to be more efficient and practical. The number of iterations required to obtain a solution is independent of the system size, but more functional evaluations are required at each iteration. In fast decupled, the number of iterations is a function of system size.

e. Because of its quadratic convergence, Newton's method is mathematically superior to the Fast - Decupled method, i.e. the number of iteration are less in Newton-Raphson.

f. The Newton-Raphson and Fast - Decupled methods using the bus admittance matrix has the advantage that the tolerances are specified for the net real and reactive powers at a bus. The tolerances, therefore, are given directly in quantities that are meaningful to the engineer who specifies the desired accuracy.

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